PROOF OF FORMULA 3.463

$$\int_0^\infty \left(e^{-x^2} - e^{-x} \right) \, \frac{dx}{x} = \frac{\gamma}{2}$$

Entry 3.476.2 states that

$$\int_0^\infty \left[\exp(-x^p) - \exp(-x^q) \right] \frac{dx}{x} = \frac{p-q}{pq} \gamma.$$

Now put p=2 and q=1 to obtain the current integral.