PROOF OF FORMULA 3.321.3

$$\int_0^\infty e^{-q^2 x^2} \, dx = \frac{\sqrt{\pi}}{2q}$$

Let t = qx to obtain

$$\int_0^\infty e^{-q^2 x^2} \, dx = \frac{1}{q} \int_0^\infty e^{-t^2} \, dt.$$

The result now follows from the value of the normal integral

$$\int_0^\infty e^{-t^2} \, dt = \frac{\sqrt{\pi}}{2}.$$