FORMULA 3.432.1

$$\int_0^\infty x^{\nu-1} e^{-mx} (e^{-x} - 1)^n \, dx = \Gamma(\nu) \sum_{k=0}^{n} (-1)^k \binom{n}{k} \frac{1}{(n+m-k)^\nu}$$