## PROOF OF FORMULA 3.419.2

$$\int_{-\infty}^{\infty} \frac{x \, dx}{(\beta + e^x)(1 - e^{-x})} = \frac{\pi^2 + \ln^2 \beta}{2(\beta + 1)}$$

In Part 1, it has been shown that

$$h_n(a) = \int_0^\infty \frac{\ln^{n-1} t \, dt}{(t-1)(t+a)}$$

is given by

$$n(1+a)h_n(a) = (-1)^n n! \left[1 + (-1)^n\right] \zeta(n)$$

$$+ \sum_{j=0}^{\lfloor n/2 \rfloor} \binom{n}{2j} \left(2^{2j} - 2\right) (-1)^{j-1} B_{2j} \pi^{2j} \ln^{n-2j} a.$$

The change of variables  $t = e^{-x}$  shows that

$$h_n(a) = \int_{-\infty}^{\infty} \frac{x^{n-1} dx}{(1 - e^{-x})(a + e^{-x})}.$$

The present entry corresponds to the value n=2.