FORMULA 4.227.5

$$\int_0^{\pi/2} \ln^{2n} \tan x \, dx = 2(2n)! \sum_{k=0}^\infty \frac{(-1)^k}{(2k+1)^{2n+1}}$$
$$= \left(\frac{\pi}{2}\right)^{2n+1} |E_{2n}| \text{ if } n \text{ is even}$$