FORMULA 4.231.16

$$\int_0^1 \ln x \, \frac{1-x^{2n+2}}{(1-x^2)^2} \, dx = -(n+1)\frac{\pi^2}{8} + \sum_{k=1}^{n} \frac{n-k+1}{(2k-1)^2}$$