PROOF OF FORMULA 4.241.8

$$\int_{1}^{\infty} \frac{\ln x \, dx}{x^2 \sqrt{x^2 - 1}} = 1 - \ln 2$$

Let $t = e^x$ to obtain

$$\int_{1}^{\infty} \frac{\ln x \, dx}{x^2 \sqrt{x^2 - 1}} = \int_{0}^{\infty} \frac{t e^{-t} \, dt}{\sqrt{e^{2t} - 1}}.$$

This last integral is evaluated in 3.452.4.