FORMULA 4.272.7

$$\int_0^1 \left(\ln \frac{1}{x} \right)^{n-1/2} x^{\nu-1} dx = \frac{(2n-1)!!}{(2\nu)^n} \sqrt{\frac{\pi}{\nu}}$$