PROOF OF FORMULA 3.222.1

$$\int_0^1 \frac{x^{a-1} \, dx}{1+x} = \beta(a)$$

This is the definition of the incomplete beta function β .