PROOF OF FORMULA 3.222.1

$$
\int_{0}^{1} \frac{x^{a-1} d x}{1+x}=\beta(a)
$$

This is the definition of the incomplete beta function $\beta$.

