

**FORMULA 4.222.4**

$$\int_0^\infty \ln(1 + a^2 x^2) \ln\left(1 + \frac{b^2}{x^2}\right) dx = 2\pi \left[ \frac{1 + ab}{a} \ln(1 + ab) - b \right]$$