NEW FORMULA 4.295.1

The original formula is

$$\int_0^\infty \frac{\ln(\mu x^2 + \beta)}{\gamma + x^2} \, dx = \frac{\pi}{\sqrt{\gamma}} \ln(\sqrt{\mu \gamma} + \sqrt{\beta})$$

 $\int_0^\infty \frac{\ln(\mu x^2 + \beta)}{\gamma + x^2} \, dx = \frac{\pi}{\sqrt{\gamma}} \ln(\sqrt{\mu \gamma} + \sqrt{\beta})$ Let $x = \sqrt{\gamma} \, t$ and replace $\mu \gamma$ by a and β by b to obtain (after writing x for the new variable of integration)

$$\int_0^\infty \frac{\ln(ax^2+b)}{1+x^2} dx = \pi \, \ln(\sqrt{a} + \sqrt{b})$$